

4R Factoring Method for Quadratics of the Form:

$$ax^2 + bx + c \text{ (when } a \text{ is not 1)}$$

THE BASIC STEPS:

- Step 1: **Remove** the a, but don't throw it away!
Step 2: Multiply $a \cdot c$.
Step 3: **Replace** c with the result of step 2 ($a \cdot c$).
Step 4: Factor the new polynomial (no a, and c is now $a \cdot c$). Factoring means making ()().
Step 5: **Replace** the a as coefficient to the x in BOTH sets of parentheses.
Step 6: **Reduce** (common factor) the sets of parentheses, if possible.
Step 7: Use FOIL to check to be certain you are correct.
-

EXAMPLE 1: $2x^2 - 7x + 6$

- Step 1: **Remove** the 2.
Step 2: Multiply $a \cdot c = 2 \cdot 6 = 12$.
Step 3: **Replace** c with 12 (the result of step 2), which makes $x^2 - 7x + 12$.
Step 4: Factor the new polynomial: $x^2 - 7x + 12 = (x - 4)(x - 3)$.
Step 5: **Replace** the a as coefficient to both x's: $(2x - 4)(2x - 3)$.
Step 6: **Reduce** (common factor) the sets of parentheses, if possible. $(2x - 4)$ can be reduced by 2, so it becomes $(x - 2)$. The other one, $(2x - 3)$, can't be reduced. This gives a final factoring of $(x - 2)(2x - 3)$.
Step 7: Use FOIL to check to be certain you are correct.
-

EXAMPLE 2: $6x^2 + 11x - 2$

- Step 1: **Remove** the 6.
Step 2: Multiply $a \cdot c = 6 \cdot (-2) = -12$.
Step 3: **Replace** c with -12 (the result of step 2), which makes $x^2 + 11x - 12$.
Step 4: Factor the new polynomial: $x^2 + 11x - 12 = (x + 12)(x - 1)$.
Step 5: **Replace** the a as coefficient to both x's: $(6x + 12)(6x - 1)$.
Step 6: **Reduce** (common factor) the sets of parentheses, if possible. $(6x + 12)$ can be reduced by 6, so it becomes $(x + 2)$. The other one, $(6x - 1)$, can't be reduced. This gives a final factoring of $(x + 2)(6x - 1)$.
Step 7: Use FOIL to check to be certain you are correct.